

## EXTRA WORKED OUT Q&A FOR STUDY UNIT 5

9. The initial temperature of a 344-g sample of iron is 18.2 °C. If the sample absorbs 2.25 kJ of energy as heat, what is its final temperature?

$0.449 \text{ J/g}\cdot\text{K} = 0.000449 \text{ kJ/g}\cdot\text{K}$

$$q = C + m \times \Delta T$$

$2.25 \text{ kJ}$        $344 \text{ g}$        $\Delta T = T_f - T_i$   
 $= T_f - 18.2^\circ\text{C}$

You can get the heat capacity of metals/elements in tables or web.

$$q = C + m \times \Delta T$$
$$2.25 \text{ kJ} = (0.000449 \text{ kJ/g}\cdot\text{K})(344 \text{ g})(T_f - 18.2)$$
$$= 0.154 \text{ kJ/K} (T_f - 18.2)$$
$$= 0.154 T_f - 2.80$$
$$T_f = \frac{2.25 + 2.80}{0.154}$$
$$= 32.79^\circ\text{C}$$

→ (You can work in K and convert to °C as well)

11. A 45.5-g sample of copper at 99.8 °C is dropped into a beaker containing 152 g of water at 18.5 °C. What is the final temperature when thermal equilibrium is reached?

*I will supply you with these values*

For Copper ( $q_1$ ) *C for Cu = 0.385 J/g·K*

\*  $q_1 = C \times m \times \Delta T$

For Water ( $q_2$ ) *C for H<sub>2</sub>O = 4.184 J/g·K*

\*  $q_2 = C \times m \times \Delta T$

Law of conservation of energy and we assume a closed system.

∴  $q_1 + q_2 = 0$

∴  $[C_{Cu} \times m_{Cu} \times (T_f - T_i)] + [C \times m \times (T_f - T_i)]_{H_2O} = 0$

$[(0.385)(45.5)(T_f - 99.8)] + [(4.184)(152)(T_f - 18.5)] = 0$

$17.52T_f - 1748.25 + 635.97T_f - 11765.41 = 0$

$653.49T_f - 13513.66 = 0$

$T_f = \frac{13513.66}{653.49}$

$T_f = 20.68^\circ\text{C}$  →



17. How much energy is evolved as heat when 1.0 L of water at 0 °C solidifies to ice? (The heat of fusion of water is 333 J/g.)

Remember that while a phase change takes place, the heat energy ( $q$ ) that is absorbed/evolved is used to establish the change in phase and not to raise/lower the temp.

Normally:  $q = C + m \times \Delta T$  / in this question a phase change takes place.  $H_2O(l) \rightarrow H_2O(s)$

So, there is no change in temp. ( $\Delta T$ ). The heat that is evolved establishes this change in phase from  $H_2O(l) \rightarrow H_2O(s)$ .

$\therefore q = C + m$  (No  $\Delta T$ ); the  $m = \text{mass}$   
 $= 333 \text{ J/g} \times 1000 \text{ g}$  of water. You have 1.00 L  
 $= 333000 \text{ J}$  of water = 1 kg  $H_2O$  or  
 or  $= 333 \text{ kJ}$  1000 g  $H_2O$ . Keep your  
 unit the same.  $C = 333 \text{ J/g}$   
 so, change mass of  $H_2O$   
 to gram.

The answer of 330 kJ is just because they used a different density for water. The density of water changes slightly with temp and pressure. The most accepted value internationally is 1 g/mL.

They probably used 0.99 g/mL which will be 990 g/Litre.

If so, then:  $q = C + m = 330 \text{ J/g} + 990 \text{ g}$   
 $= 329670 \text{ J}$   
 $= 329.67 \text{ kJ}$   
 $\approx 330 \text{ kJ}$ .

- liquid water at 0 °C:
19. How much energy is required to vaporize 125 g of benzene,  $C_6H_6$ , at its boiling point,  $80.1\text{ }^\circ\text{C}$ ? (The heat of vaporization of benzene is  $30.8\text{ kJ/mol}$ .)

$$\begin{aligned}q &= C \times m \\ &= (30.8\text{ kJ/mol})(1.60\text{ mol}) \\ &= \underline{49.31\text{ kJ}}\end{aligned}$$

The question is only to vaporize. So, there is no heating or cooling first to the vaporization point.

$$125\text{ g } C_6H_6 = \frac{125\text{ g}}{78.06\text{ g}\cdot\text{mol}^{-1}} = \underline{1.60\text{ mol}}$$

- \* We use mol because the heat capacity for benzene ( $C$ ) was given in  $\text{kJ}/\underline{\underline{\text{mol}}}$ .
- \* Always watch your units.



21. The freezing point of mercury is  $-38.8\text{ }^{\circ}\text{C}$ . What quantity of energy, in joules, is released to the surroundings if  $1.00\text{ mL}$  of mercury is cooled from  $23.0\text{ }^{\circ}\text{C}$  to  $-38.8\text{ }^{\circ}\text{C}$  and then frozen to a solid? (The density of liquid mercury is  $13.6\text{ g/cm}^3$ . Its specific heat capacity is  $0.140\text{ J/g}\cdot\text{K}$  and its heat of fusion is  $11.4\text{ J/g}$ .)

To cool and freeze the mercury is a 2-step process. Step 1 involves cooling the mercury to its freezing point. Heat is given off.  
Step 2 involves a change of state. So, temp will stay constant = no  $\Delta T$ .

Step 1:  $q_1 = c \times m \times \Delta T$

$$m_{\text{Hg}} = d \times V = 13.6\text{ g/cm}^3 \times 1\text{ cm}^3 = \underline{13.6\text{ g}}$$

$$\Delta T = T_f - T_i = -38.8^{\circ}\text{C} - 23.0^{\circ}\text{C} \\ = \underline{-61.8^{\circ}\text{C}}$$

$$\therefore q_1 = (0.140\text{ J/g}\cdot\text{K})(13.6\text{ g})(-61.8^{\circ}\text{C}) \\ = \underline{-117.67\text{ J}}$$

\* Step 2:  $q_2 = c \times m$   
 $= (11.4\text{ J/g})(13.6\text{ g})$   
 $= \underline{155.04\text{ J}}$

\* Total energy  $= q_1 + q_2$   
 $= 117.67\text{ J} + 155.04\text{ J}$   
 $= \underline{272.71\text{ J}}$

Remember that the minus sign only indicates that it is an exothermic process. It is not a negative value, therefore you use it as a  $\oplus$  value in adding to the  $q_2$ .