

ANSWER TO "TRY YOURSELF" PROBLEM FROM STUDY SECTION 9.2

Try Yourself 9.2a

Calculate the pH of a buffer solution with 0.5 mol/L HCOOH and 0.7 mol/L HCOO⁻. K_a for formic acid (metanoic acid) = 1.8 × 10⁻⁴.

Try Yourself 9.2 a

$$\text{pH} = \text{pK}_a + \log \frac{[\text{A}^-] \dots \rightarrow \text{Base}}{[\text{HA}] \dots \rightarrow \text{Acid}}$$
$$K_a = 1.8 \times 10^{-4}$$
$$\therefore \text{pK}_a = -\log 1.8 \times 10^{-4} = 3.74 \rightarrow$$
$$\therefore \text{pH} = \text{pK}_a + \log \frac{[\text{HCOO}^-]}{[\text{HCOOH}]}$$
$$= 3.74 + \log \frac{[0.7]}{[0.5]}$$
$$= 3.74 + 0.15$$
$$= 3.89 \rightarrow$$

Try Yourself 9.2b

You wish to prepare 1000 mL of a buffer solution with a pH of 10.50

A list of possible acids (and their conjugated bases) follows:

| Acid | Conjugate base | K_a |
|--------------------------------------|---------------------------------|-----------------------|
| Benzoic acid ($C_6H_5CO_2H$) | Benzoate ion ($C_6H_5CO_2^-$) | 6.3×10^{-5} |
| Hydrogen sulfide (H_2S) | Hydrogen sulfide ion (HS^-) | 1×10^{-7} |
| Ammonium ion (NH_4^+) | Ammonia (NH_3) | 5.6×10^{-10} |
| Hydrogen carbonate ion (HCO_3^-) | Carbonate ion (CO_3^{2-}) | 4.8×10^{-11} |

Which combination should be selected and what should be the ratio of acid to conjugate base?

Answer:

Try Yourself 9.2b

Calculate pK_a values of the acids.

- 1) Benzoic acid, $K_a = 6.3 \times 10^{-5} \Rightarrow pK_a = 4.20$
- 2) Hydrogen sulfide, $K_a = 1 \times 10^{-7} \Rightarrow pK_a = 7.00$
- 3) Ammonium ion, $K_a = 5.6 \times 10^{-10} \Rightarrow pK_a = 9.25$
- 4) Hydrogen carbonate ion, $K_a = 4.8 \times 10^{-11} \Rightarrow pK_a = 10.32$

Use acid no. 4: Hydrogen carbonate because pK_a value is closest to pH

$$pH = pK_a + \log \frac{[Base]}{[Acid]}$$
$$\log \frac{[Carbonate\ ion]}{[Hydrogen\ carbonate\ ion]} + pK_a = pH$$
$$\log \frac{[CO_3^{2-}]}{[HCO_3^-]} = 10.50 - 10.32 = 0.18$$
$$\therefore \frac{[CO_3^{2-}]}{[HCO_3^-]} = 10^{0.18} = 1.51$$

\therefore mol ratio of base : acid = 1.51 : 1

\therefore So, you will use 1.51 mol of a base salt like sodium carbonate (Na_2CO_3) and an acidic salt like sodium hydrogen carbonate ($NaHCO_3$) 1 mol.

$\therefore M_{Na_2CO_3} = n \times M = 1.51 \text{ mol} \times \frac{106}{1000} \text{ g mol}^{-1} = 160.06 \text{ g}$

$M_{NaHCO_3} = n \times M = 1 \text{ mol} \times 84.01 \text{ g mol}^{-1} = 84.01 \text{ g}$

Dissolve 160.06 g of Na_2CO_3 and 84.01 g of $NaHCO_3$ in enough water to make up 1L solution.